

## Absolute Value Equations

Solve each equation.

1)  $|n| = 2$

$\{-2, 2\}$

2)  $|8n| = -32$

$\boxed{\text{NS}}$

3)  $|3k| = 9$

$\frac{3k}{3} = \frac{9}{3}$

$k = 3$

$|3(3)| = 9$   
 $9 = 9 \checkmark$

$\frac{3k}{3} = \frac{-9}{3}$

$k = -3$

$|3(-3)| = 9$   
 $9 = 9 \checkmark$

$\boxed{\{-3, 3\}}$

4)  $|7n| = 56$

$\frac{7n}{7} = \frac{56}{7}$

$n = 8$

$|7(8)| = 56$   
 $56 = 56 \checkmark$

$\frac{7n}{7} = \frac{-56}{7}$

$n = -8$

$|7(-8)| = 56$   
 $56 = 56 \checkmark$

$\boxed{\{-8, 8\}}$

5)  $\left| \frac{x}{4} - 2 \right| = -2$

$\left| \frac{x}{4} \right| = 0$

$\frac{x}{4} = 0 \cdot 4$

$x = 0$

$\left| \frac{0}{4} \right| = 0$   
 $0 = 0 \checkmark$

$\boxed{\{0\}}$

6)  $\left| \frac{p+8}{7} \right| = -3 \cdot 7$

$|p+8| = -21$

$\boxed{\text{NS}}$

7)  $\left| \frac{x+2}{3} \right| = 4 \cdot 3$

$|x+2| = 12$

$x+2 = 12$   
 $\frac{x}{1} = \frac{10}{1}$

$x = 10$

$|10+2| = 12$   
 $12 = 12 \checkmark$

$x+2 = -12$   
 $\frac{x}{1} = \frac{-14}{1}$

$x = -14$

$|(-14)+2| = 12$   
 $12 = 12 \checkmark$

$\boxed{\{-14, 10\}}$

8)  $|-3v| + 1 = 10$

$|-3v| = 9$

$\frac{-3v}{-3} = \frac{9}{-3}$

$v = -3$

$|-3(-3)| = 9$   
 $9 = 9 \checkmark$

$\frac{-3v}{-3} = \frac{-9}{-3}$

$v = 3$

$|-3(3)| = 9$   
 $9 = 9 \checkmark$

$\boxed{\{-3, 3\}}$

9)  $|-n+7| = 0$

$-n+7 = 0$

$-n = -7$

$\frac{-n}{-1} = \frac{-7}{-1}$

$n = 7$

$|-7+7| = 0$   
 $0 = 0 \checkmark$

$\boxed{\{7\}}$

10)  $|-7-5r| = 23$

$-7-5r = 23$   
 $\frac{-5r}{-5} = \frac{30}{-5}$

$r = -6$

$|-7-5(-6)| = 23$   
 $|-7+30| = 23$   
 $23 = 23 \checkmark$

$-7-5r = -23$   
 $\frac{-5r}{-5} = \frac{-16}{-5}$

$r = \frac{16}{5}$

$|-7-5(\frac{16}{5})| = 23$   
 $|-7-16| = 23$   
 $|-23| = 23 \checkmark$

$\boxed{\{-6, \frac{16}{5}\}}$

$$11) |4b - 10| = 26$$

$$4b - 10 = 26$$

$$\begin{array}{r} +16 \\ \hline 4b = 36 \\ \frac{4b}{4} = \frac{36}{4} \\ b = 9 \end{array}$$

$$4b - 10 = -26$$

$$\begin{array}{r} +16 \\ \hline 4b = -16 \\ \frac{4b}{4} = \frac{-16}{4} \\ b = -4 \end{array}$$

$$|4(9) - 10| = 26$$

$$|36 - 10| = 26$$

$$26 = 26 \checkmark$$

$$|4(-4) - 10| = 26$$

$$|-16 - 10| = 26$$

$$-26 = 26$$

$$\boxed{\{-4, 9\}}$$

$$13) 4|8 - 7r| + 8 = 116$$

$$\begin{array}{r} -8 \\ \hline 4|8 - 7r| = 108 \\ \frac{4|8 - 7r|}{4} = \frac{108}{4} \end{array}$$

$$|8 - 7r| = 27$$

$$8 - 7r = 27$$

$$\begin{array}{r} -8 \\ \hline -7r = 19 \\ \frac{-7r}{-7} = \frac{19}{-7} \\ r = -\frac{19}{7} \end{array}$$

$$8 - 7r = -27$$

$$\begin{array}{r} -8 \\ \hline -7r = -35 \\ \frac{-7r}{-7} = \frac{-35}{-7} \\ r = 5 \end{array}$$

$$|8 - 7(-\frac{19}{7})| = 27$$

$$|8 + 19| = 27$$

$$27 = 27 \checkmark$$

$$|8 - 7(5)| = 27$$

$$|8 - 35| = 27$$

$$|-27| = 27 \checkmark$$

$$\boxed{\{-\frac{19}{7}, 5\}}$$

$$15) 2 - 6|2v + 2| = -70$$

$$\begin{array}{r} -2 \\ \hline -6|2v + 2| = -72 \\ \frac{-6|2v + 2|}{-6} = \frac{-72}{-6} \end{array}$$

$$|2v + 2| = 12$$

$$2v + 2 = 12$$

$$\begin{array}{r} -2 \\ \hline 2v = 10 \\ \frac{2v}{2} = \frac{10}{2} \\ v = 5 \end{array}$$

$$2v + 2 = -12$$

$$\begin{array}{r} -2 \\ \hline 2v = -14 \\ \frac{2v}{2} = \frac{-14}{2} \\ v = -7 \end{array}$$

$$|2(5) + 2| = 12$$

$$|10 + 2| = 12$$

$$|12| = 12 \checkmark$$

$$|2(-7) + 2| = 12$$

$$|-14 + 2| = 12$$

$$|-12| = 12 \checkmark$$

$$\boxed{\{-7, 5\}}$$

$$12) |9x - 2| = 88$$

$$9x - 2 = 88$$

$$\begin{array}{r} +2 \\ \hline 9x = 90 \\ \frac{9x}{9} = \frac{90}{9} \\ x = 10 \end{array}$$

$$|9(10) - 2| = 88$$

$$|90 - 2| = 88$$

$$88 = 88 \checkmark$$

$$\boxed{\{-\frac{86}{9}, 10\}}$$

$$9x - 2 = -88$$

$$\begin{array}{r} +2 \\ \hline 9x = -86 \\ \frac{9x}{9} = \frac{-86}{9} \\ x = -\frac{86}{9} \end{array}$$

$$|9(-\frac{86}{9}) - 2| = 88$$

$$|-86 - 2| = 88$$

$$88 = 88 \checkmark$$

$$\boxed{\{0, 3\}}$$

$$14) 8|-9 + 6r| + 5 = 77$$

$$\begin{array}{r} -5 \\ \hline 8|-9 + 6r| = 72 \\ \frac{8|-9 + 6r|}{8} = \frac{72}{8} \end{array}$$

$$|-9 + 6r| = 9$$

$$-9 + 6r = 9$$

$$\begin{array}{r} +9 \\ \hline 6r = 18 \\ \frac{6r}{6} = \frac{18}{6} \\ r = 3 \end{array}$$

$$-9 + 6r = -9$$

$$\begin{array}{r} +9 \\ \hline 6r = 0 \\ \frac{6r}{6} = \frac{0}{6} \\ r = 0 \end{array}$$

$$|-9 + 6(3)| = 9$$

$$|-9 + 18| = 9$$

$$|9| = 9 \checkmark$$

$$|-9 + 6(0)| = -9$$

$$|-9| = 9 \checkmark$$

$$16) 5|7r + 8| - 10 = -75$$

$$\begin{array}{r} +10 \\ \hline 5|7r + 8| = -65 \\ \frac{5|7r + 8|}{5} = \frac{-65}{5} \end{array}$$

$$|7r + 8| = -13$$

$$\boxed{NS}$$