

Power {  $2 \leftarrow$  Base  $4 \leftarrow$  Exponent } Properties of Exponents

Definitions:

1. Product of Power Property -  $a^m \cdot a^n = a^{m+n}$

ex.  $5^3 \cdot 5^{-1} = 5^2$

2. Power of a Power Property -  $(a^m)^n = a^{mn}$

ex.  $(3^3)^2 = 3^6$

3. Power of a Product Property -  $(ab)^m = a^m b^m$

ex.  $(2 \cdot 3)^4 = 2^4 \cdot 3^4$

4. Negative Exponent Property -  $a^{-m} = \frac{1}{a^m}$

ex.  $7^{-2} b^3 = \frac{b^3}{7^2}$

5. Zero Exponent Property -  $a^0 = 1, a \neq 0$

ex.  $(-89m^2n^{-3})^0 = 1$

6. Quotient of Powers Property -  $\frac{a^m}{a^n} = a^{m-n}$

ex.  $\frac{6^{-3}}{6^{-6}} = 6^3$

7. Power of a Quotient Property -  $\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$

ex.  $\left(\frac{4}{7}\right)^2 = \frac{4^2}{7^2}$

Example 1.)  $(-4^1 \cdot 2^5)^2$   
 $(-4)^2 \cdot 2^{10}$

Example 2.)  $\left(\frac{11^5}{11^8}\right)^{-1} = (11^{-3})^{-1} = 11^3$

$\frac{11^{-5}}{11^{-8}} = 11^3$

$\frac{11^8}{11^5} = 11^3$

Example 3.)  $b^{-4} b^6 b^7$

$b^9$

Example 4.)  $\left(\frac{r^{-2}}{s^3}\right)^{-3}$

$\frac{r^6}{s^{-9}} = r^6 s^9$

Example 5.)  $\frac{16m^4n^{-5}}{2n^{-5}}$

$8m^4$

$$\frac{4x^3 + 6x^2 - 4x + 2}{-1}$$

$-1$

$$-4x^3 - 6x^2 + 4x - 2$$

1.  $\frac{1}{-3x^{-4}}$   
 $\frac{x^4}{-3} = \boxed{\frac{-x^4}{3}}$

2.  $\left(\frac{2x^2}{y}\right)^3$

$$\frac{8x^6}{y^3}$$

3.  $4x^3 \cdot 5x^{-3} \cdot x^7$

$$20x^7$$

4.  $\frac{w^{-4}}{w^4}$

5.  $y \cdot y^5 \cdot y^3$

6.  $(-x)^3(-x)^{13}$

7.  $\frac{x^{12}}{1} \cdot \frac{3}{x^{20}}$   
 $\frac{3x^{12}}{x^{20}}$

8.  $(7x^{-3}y^7z)^0$

$1$

9.  $(-5x^6y)^2(-x^2)$

$\frac{3}{x^8}$

10.  $\left(\frac{8x^6y^7}{4x^4y^5}\right)^3 \cdot \left(\frac{5x^9y}{x^3y^5}\right)^{-2}$

11.  $[(x+3)^2]^4$   
 $(x+3)^8$

12.  $\left(\frac{2x^3}{y}\right)^3 \cdot \frac{1}{-6x^3}$

$$\left(\frac{2x^3}{y^3}\right)^3 \cdot \left(\frac{5x^6}{y^4}\right)^{-2}$$

$$\frac{8x^9}{y^9} \cdot \frac{y^8}{25x^{12}} = \frac{8x^9y^8}{25x^{12}y^9} = \frac{8}{25x^3y}$$