

Quadratic Review #2

Solve each equation by factoring.

1) $b^2 + 4 = -5b$

$b^2 + 5b + 4 = 0$

$(b+4)(b+1) = 0$

$b = -4, -1$

2) $n^2 - 12 = n$

$n^2 - n - 12 = 0$

$(n-4)(n+3) = 0$

$n = 4, -3$

3) $n^2 + 10 = 7n$

$n^2 - 7n + 10 = 0$

$(n-5)(n-2) = 0$

$n = 5, 2$

Solve each equation by completing the square.

4) $b^2 - 10b - 73 = -7$

$b^2 - 10b = 66$

$b^2 - 10b + 25 = 66 + 25$

$(b-5)^2 = 91$

$b-5 = \pm\sqrt{91}$

$b = 5 \pm \sqrt{91}$

6) $9n^2 - 18n - 53 = 3$

$9n^2 - 18n = 56$

$9(n^2 - 2n) = 56$

$9(n^2 - 2n + 1) = 56 + 9$

$9\left(\frac{n-1}{3}\right)^2 = \frac{65}{3}$

$\sqrt{\left(\frac{n-1}{3}\right)^2} = \sqrt{\frac{65}{9}}$

$\frac{n-1}{3} = \pm\sqrt{\frac{65}{9}}$

$n-1 = \pm\sqrt{\frac{65}{3}}$

$n = 1 \pm\sqrt{\frac{65}{3}}$

5) $8x^2 + 16x - 35 = 7$

$8x^2 + 16x = 42$

$8(x^2 + 2x) = 42$

$8(x^2 + 2x + 1) = 42 + 8$

$\frac{8(x+1)^2}{8} = \frac{50}{8}$

$\sqrt{(x+1)^2} = \sqrt{\frac{25}{4}}$

$x+1 = \pm\frac{5}{2}$

$x = -1 \pm\frac{5}{2}$

$x = -\frac{2}{2} \pm\frac{5}{2}$

$x = \frac{3}{2}, -\frac{7}{2}$

Solve each equation with the quadratic formula.

7) $12m^2 = 12m + 22$

$12m^2 - 12m - 22 = 0$

$x = \frac{12 \pm \sqrt{(-12)^2 - 4(12)(-22)}}{2(12)}$

$= \frac{12 \pm \sqrt{1200}}{24}$

$x = \frac{3 \pm 5\sqrt{3}}{6}$

9) $9x^2 + 3 = 7x$

$9x^2 - 7x + 3 = 0$

$x = \frac{7 \pm \sqrt{(-7)^2 - 4(9)(3)}}{2(9)}$

$= \frac{7 \pm \sqrt{-59}}{18}$

$x = \frac{7 \pm i\sqrt{59}}{18}$

8) $n^2 = -11n + 102$

$n^2 + 11n - 102 = 0$

$x = \frac{-11 \pm \sqrt{(11)^2 - 4(1)(-102)}}{2(1)}$

$= \frac{-11 \pm \sqrt{529}}{2}$

$= \frac{-11 \pm 23}{2}$

$x = 6, -17$

$$\begin{aligned} \textcircled{1} \quad & -16x^2 + 72x + 88 = 0 \\ & -8(2x^2 - 9x - 11) = 0 \\ & 2x^2 - 11x + 2x - 11 \\ & x(2x - 11) + (2x - 11) \\ & -8(2x - 11)(x + 1) = 0 \\ & \boxed{x = \frac{11}{2}, -1} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad & A = lw \\ & 54 = (2w - 3)(w) \\ & 54 = 2w^2 - 3w \quad 108 \\ & 2w^2 - 3w - 54 = 0 \\ & 2w^2 - 12w + 9w - 54 \\ & 2w(w - 6) + 9(w - 6) \\ & (2w + 9)(w - 6) = 0 \\ & \boxed{w = \frac{-9}{2}, 6} \quad \boxed{w = 6 \quad l = 9} \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad & 30 = (s + 3)(s + 2) \\ & 30 = s^2 + 2s + 3s + 6 \\ & 30 = s^2 + 5s + 6 \\ & s^2 + 5s - 24 = 0 \\ & (s + 8)(s - 3) = 0 \\ & \boxed{s = -8, 3} \quad \boxed{s = 3 \text{ ft}} \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad & (s + 5)(s + 12) = 120 \\ & s^2 + 12s + 5s + 60 = 120 \\ & s^2 + 17s - 60 = 0 \\ & (s + 20)(s - 3) = 0 \\ & \boxed{s = -20, 3} \quad \boxed{8 \times 15} \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad & (x + 5)(x + 6) = 72 \\ & x^2 + 5x + 6x + 30 = 72 \\ & x^2 + 11x - 42 = 0 \\ & (x + 14)(x - 3) = 0 \\ & \boxed{x = -14, 3} \quad \begin{array}{l} \text{3 total feet} \\ \text{1.5 for 1 side} \end{array} \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad & h = -16t^2 + 8t + 80 \\ & -8(2t^2 - t - 10) = h \\ & -8(2t^2 - 5t + 4t - 10) \\ & t(2t - 5) + 2(t - 5) \\ & -8(2t - 5)(t + 2) = 0 \\ & \boxed{t = \frac{5}{2}, -2} \quad \boxed{t = 2.5 \text{ s}} \end{aligned}$$

$$\begin{aligned} * \textcircled{7} \quad & 10 = -16t^2 + 50t + 4 \\ & -16t^2 + 50t - 6 = 0 \\ & -2(8t^2 - 25t + 3) = 0 \\ & -2(8t^2 - 24t - 1t + 3) = 0 \\ & 8t(t - 3) - 1(t - 3) \\ & -2(8t - 1)(t - 3) = 0 \\ & \boxed{t = \frac{1}{8}, 3} \quad \boxed{3 \text{ sec}} \end{aligned}$$

$$\begin{aligned} \textcircled{8} \quad & 13 = -16t^2 + 36t + 5 \\ & -16t^2 + 36t - 8 = 0 \\ & -2(8t^2 - 18t + 4) = 0 \\ & -2(8t^2 - 16t - 2t + 4) = 0 \\ & 8t(t - 2) - 2(t - 2) \\ & -2(8t - 2)(t - 2) = 0 \\ & \boxed{t = \frac{1}{4}, 2} \quad \boxed{2 \text{ seconds}} \end{aligned}$$