

Solving by Factoring

Solve each equation by factoring.

1) $(x+3)(6x-1)=0$

$$\begin{array}{r} x+3=0 \\ -3 \quad -3 \\ \hline \end{array}$$

$$x = -3$$

$$x = -3, \frac{1}{6}$$

$$\begin{array}{r} 6x-1=0 \\ +1 \quad +1 \\ \hline \end{array}$$

$$\frac{6x}{6} = \frac{1}{6}$$

$$x = \frac{1}{6}$$

2) $x(x+4)=0$

$$x = 0$$

$$\begin{array}{r} x+4=0 \\ -4 \quad -4 \\ \hline \end{array}$$

$$x = -4$$

$$x = 0, -4$$

3) $x^2 - 3x = 0$

$$x(x-3)=0$$

$$x = 0$$

$$\begin{array}{r} x-3=0 \\ +3 \quad +3 \\ \hline \end{array}$$

$$x = 3$$

$$x = 0, 3$$

4) $x^2 + 11x + 28 = 0$

$$x^2 + 7x + 4x + 28$$

$$x(x+7) \quad 4(x+7)$$

$$(x+4)(x+7)=0$$

$$x = -4, -7$$

$$\begin{array}{r} x+4=0 \\ -4 \quad -4 \\ \hline \end{array}$$

$$x = -4$$

$$\begin{array}{r} x+7=0 \\ -7 \quad -7 \\ \hline \end{array}$$

$$x = -7$$

5) $v^2 + 4v - 21 = 0$

$$v^2 + 7v - 3v - 21$$

$$v(v+7) - 3(v+7)$$

$$(v+7)(v-3)=0$$

$$v = -7, 3$$

$$\begin{array}{r} v+7=0 \\ -7 \quad -7 \\ \hline \end{array}$$

$$\begin{array}{r} v-3=0 \\ +3 \quad +3 \\ \hline \end{array}$$

$$v = -7 \quad v = 3$$

6) $r^2 + 10r + 21 = 0$

$$(r+7)(r+3)=0$$

$$\begin{array}{r} r+7=0 \\ -7 \quad -7 \\ \hline \end{array}$$

$$r = -7$$

$$\begin{array}{r} r+3=0 \\ -3 \quad -3 \\ \hline \end{array}$$

$$r = -3$$

$$r = -7, -3$$

7) $p^2 + p - 39 = 0$

$$p^2 + p - 42 = 0$$

$$(p+7)(p-6)=0$$

$$p = -7, 6$$

$$\begin{array}{r} p+7=0 \\ -7 \quad -7 \\ \hline \end{array}$$

$$\begin{array}{r} p-6=0 \\ +6 \quad +6 \\ \hline \end{array}$$

$$p = -7$$

$$p = 6$$

8) $v^2 - 23 = -7$

$$v^2 - 16 = 0$$

$$(v+4)(v-4)=0$$

$$v = 4, -4$$

$$\begin{array}{r} v+4=0 \\ -4 \quad -4 \\ \hline \end{array}$$

$$v = -4$$

$$\begin{array}{r} v-4=0 \\ +4 \quad +4 \\ \hline \end{array}$$

$$v = 4$$

9) $x^2 = 2x$

$$-2x - 2x$$

$$x^2 - 2x = 0$$

$$x(x-2)=0$$

$$x = 0, 2$$

$$x = 0$$

$$\begin{array}{r} x-2=0 \\ +2 \quad +2 \\ \hline \end{array}$$

$$x = 2$$

10) $k^2 = 30 + k$

$$k^2 - k - 30 = 0$$

$$(k-6)(k+5)=0$$

$$k = 6, -5$$

$$\begin{array}{r} k-6=0 \\ +6 \quad +6 \\ \hline \end{array}$$

$$k = 6$$

$$\begin{array}{r} k+5=0 \\ -5 \quad -5 \\ \hline \end{array}$$

$$k = -5$$

$$11) 3m^2 + 14m + 48 = 2m^2$$

$$\begin{array}{r} -2m^2 \\ \hline m^2 + 14m + 48 = 0 \end{array}$$

$$(m+8)(m+6) = 0$$

$$m+8=0 \quad m+6=0$$

$$\boxed{m = -8, -6}$$

$$13) 2r^2 - 9r + 9 = 0$$

$$2r^2 - 3r - 6r + 9$$

$$r(2r-3) - 3(2r-3)$$

$$(2r-3)(r-3) = 0$$

$$\boxed{r = \frac{3}{2}, 3}$$

$$15) 25x^2 - 5x - 6 = 0$$

$$25x^2 - 15x + 10x - 6$$

$$5x(5x-3) + 2(5x-3)$$

$$(5x-3)(5x+2) = 0$$

$$\boxed{x = \frac{3}{5}, -\frac{2}{5}}$$

$$17) 3x^2 + x + 4 = 4$$

$$\begin{array}{r} -4 \\ \hline 3x^2 + x = 0 \end{array}$$

$$x(3x+1) = 0$$

$$\boxed{x = 0, -\frac{1}{3}}$$

$$19) 5r^2 - 10 = 23r$$

$$\begin{array}{r} -23r \\ \hline 5r^2 - 23r - 10 = 0 \end{array}$$

$$5r^2 - 25r + 2r - 10$$

$$5r(r-5) + 2(r-5)$$

$$(5r+2)(r-5) = 0$$

$$\boxed{r = -\frac{2}{5}, 5}$$

$$21) 3x^2 - 4 = -4x$$

$$\begin{array}{r} +4x \\ \hline 3x^2 + 4x - 4 = 0 \end{array}$$

$$3x^2 + 6x - 2x - 4$$

$$3x(x+2) - 2(x+2)$$

$$(3x-2)(x+2) = 0$$

$$\boxed{x = \frac{2}{3}, -2}$$

$$12) v^2 + 9v + 12 = -2$$

$$\begin{array}{r} +2 \\ \hline v^2 + 9v + 14 = 0 \end{array}$$

$$(v+7)(v+2) = 0$$

$$\boxed{v = -7, -2}$$

$$14) 6p^2 - 23p + 20 = 0$$

$$6p^2 - 15p - 8p + 20$$

$$3p(2p-5) - 4(2p-5)$$

$$(3p-4)(2p-5) = 0$$

$$\boxed{p = \frac{4}{3}, \frac{5}{2}}$$

$$16) 3k^2 - 10k - 25 = 0$$

$$3k^2 - 15k + 5k - 25$$

$$3k(k-5) + 5(k-5)$$

$$(3k+5)(k-5) = 0$$

$$\boxed{k = -\frac{5}{3}, 5}$$

$$18) 4n^2 + 11n + 1 = -5$$

$$\begin{array}{r} +5 \\ \hline 4n^2 + 11n + 6 = 0 \end{array}$$

$$4n^2 + 8n + 3n + 6$$

$$4n(n+2) + 3(n+2)$$

$$(4n+3)(n+2) = 0$$

$$\boxed{n = -\frac{3}{4}, -2}$$

$$20) 5x^2 + 5 = 26x$$

$$\begin{array}{r} -26x \\ \hline 5x^2 - 26x + 5 = 0 \end{array}$$

$$5x^2 - 25x - 1x + 5$$

$$5x(x-5) - 1(x-5)$$

$$(5x-1)(x-5) = 0$$

$$\boxed{x = \frac{1}{5}, 5}$$

$$22) 10x^2 - 3x - 1 = -2x + 2$$

$$\begin{array}{r} +2x - 2 \\ \hline 10x^2 - x - 3 = 0 \end{array}$$

$$10x^2 - 6x + 5x - 3$$

$$2x(5x-3) + 1(5x-3)$$

$$(5x-3)(2x+1) = 0$$

$$\boxed{x = \frac{3}{5}, -\frac{1}{2}}$$

$$23) \sqrt{108} = 6\sqrt{3}$$

$$24) \sqrt{98} = 7\sqrt{2}$$

$$25) \sqrt{80} = 4\sqrt{5}$$

$$26) \sqrt{392} = 14\sqrt{2}$$