

Systems Review 2

Solve each system by elimination.

1) $-2r + s - t = 13$

$-r - s + t = 5$

$r + 2s - t = -9$

$(-6, -4, -5)$

$-2r + s - t = 13$

$-r - s + t = 5$

$-3r = 18$

$r = -6$

$6 + 4 + t = 5$

$10 + t = 5$

$t = -5$

$-r - s + t = 5$

$r + 2s - t = -9$

$s = -4$

2) $2x + 4y + 4z = -2$

$-6x - 4y - 4z = 14$

$2x + 4z = 2$

$(-3, -1, 2)$

$2x + 4y + 4z = -2$

$-6x - 4y - 4z = 14$

$-4x = 12$

$x = -3$

$2(-3) + 4z = 2$

$-6 + 4z = 2$

$4z = 8$

$z = 2$

$2(-3) + 4y + 4(2) = -2$

$-6 + 4y + 8 = -2$

$4y + 2 = -2$

$4y = -4$

$y = -1$

3) $x + 2y - 3z = -2$

$5x + 4y = -22$

$-6x + 3y + 3z = -3$

$(-2, -3, -2)$

$x + 2y - 3z = -2$

$-6x + 3y + 3z = -3$

$-5x + 5y = -5$

$5x + 4y = -22$

$9y = -27$

$y = -3$

$5x + 4(-3) = -22$

$5x - 12 = -22$

$5x = -10$

$x = -2$

$-2 + 2(-3) - 3(-2) = -2$

$-2 - 6 - 3(-2) = -2$

$-8 - 3(-2) = -2$

$-3(-2) = 6$

$z = -2$

4) $y - 2z = -7$

$-2x - y + 2z = 11$

$2x + y + 5z = 17$

$(-2, 1, 4)$

$-2x - y + 2z = 11$

$2x + y + 5z = 17$

$7z = 28$

$z = 4$

$y - 2(4) = -7$

$y - 8 = -7$

$y = 1$

$2x + 1 + 20 = 17$

$2x + 21 = 17$

$2x = -4$

$x = -2$

$$\begin{aligned} 5) \quad & -x - 4y - z = -13 \\ & (-x + 2y + 2z = -18) \cdot 2 \\ & -5x - 2y + 4z = -16 \end{aligned}$$

No Solution

$$\begin{aligned} -x - 4y - z &= -13 \\ -2x + 4y + 4z &= -36 \\ \hline -3x + 3z &= -49 \end{aligned}$$

$$\begin{aligned} -x + 2y + 2z &= -18 \\ -5x - 2y + 4z &= -16 \\ \hline -6x + 6z &= -34 \end{aligned}$$

$$\begin{aligned} -2(-3x + 3z) &= -98 \\ -6x + 6z &= -34 \\ 6x - 6z &= 98 \\ \hline 0 &= 64 \end{aligned}$$

$$\begin{aligned} 6) \quad & (x + 5y + 3z = -3) \cdot 5 \\ & (4x - y - 5z = -3) \cdot 3 \\ & x + 2y + 5z = -15 \end{aligned}$$

$(-4, 2, -3)$

$$\begin{aligned} 5x + 25y + 15z &= -15 \\ 12x - 3y - 15z &= -9 \\ \hline 17x + 22y &= -24 \end{aligned}$$

$$\begin{aligned} 4x - y - 5z &= -3 \\ x + 2y + 5z &= -15 \\ \hline (5x + y = -18) \cdot 22 \\ 11x + 22y &= -24 \\ -110x - 27y &= 396 \\ \hline -93x &= 372 \\ x &= -4 \end{aligned}$$

$$\begin{aligned} -4 + 10 + 3z &= -3 \\ 6 + 3z &= -3 \\ 3z &= -9 \\ z &= -3 \end{aligned}$$

$$\begin{aligned} -20 + y &= -18 \\ y &= 2 \end{aligned}$$

$$\begin{aligned} 7) \quad & (5x - 5y + 5z = 30) \cdot 4 \\ & (2x + 2y + 4z = 6) \cdot 5 \\ & 5x + 5y = 25 \end{aligned}$$

$(6, -1, -1)$

$$\begin{aligned} -20x + 20y - 20z &= -120 \\ 10x + 10y + 20z &= 30 \\ \hline -10x + 30y &= -90 \\ z(5x + 5y) &= 25 \end{aligned}$$

$$\begin{aligned} -10x + 30y &= -90 \\ 10x + 10y &= 50 \\ \hline 40y &= -40 \\ y &= -1 \end{aligned}$$

$$\begin{aligned} 30 + 5 + 5z &= 30 \\ 35 + 5z &= 30 \\ 5z &= -5 \\ z &= -1 \end{aligned}$$

$$\begin{aligned} 5x - 5 &= 25 \\ 5x &= 30 \\ x &= 6 \end{aligned}$$

$$\begin{aligned} 8) \quad & -x - 4y - 5z = 1 \\ & -4(3x - y - 3z = 5) \\ & -x + 4y - 6z = -16 \end{aligned}$$

$(2, 2, 1)$

$$\begin{aligned} -x - 4y - 5z &= 1 \\ -12x + 4y + 12z &= -20 \\ \hline -13x + 7z &= -19 \end{aligned}$$

$$\begin{aligned} 22 - 18z &= 4 \\ -18z &= -18 \\ z &= 1 \end{aligned}$$

$$\begin{aligned} 12x - 4y - 12z &= 20 \\ -x + 4y - 6z &= -16 \\ \hline (11x - 18z = 4) \cdot 7 \\ (-13x + 7z = -19) \cdot 18 \\ \hline 77x - 126z &= 28 \\ -234x + 126z &= -342 \\ \hline -157x &= -314 \end{aligned}$$

$$\begin{aligned} -2 + 4y - 6 &= -16 \\ -8 + 4y &= -16 \\ 4y &= 8 \\ y &= 2 \end{aligned}$$

$$\begin{aligned} -157x &= -314 \\ x &= 2 \end{aligned}$$

Solve each system of equations.

9) $3x^2 + 4y^2 - 96x + 3y - 22 = 0$
 $3x - y = -2 \quad y = 3x + 2$

$3x^2 + 4(3x+2)^2 - 96x + 3(3x+2) - 22 = 0$
 $3x^2 + 4(9x^2 + 12x + 4) - 96x + 9x + 6 - 22 = 0$
 $3x^2 + 36x^2 + 48x + 16 - 96x + 9x + 6 - 22 = 0$
 $39x^2 - 39x = 0$
 $39x(x-1) = 0$
 $x = 0, 1$

$y = 3(0) + 2 = 2$
 $y = 3(1) + 2 = 5$

$(0, 2), (1, 5)$

11) $2y^2 - 84x - 4y + 138 = 0$
 $3x + y = 3 \quad y = -3x + 3$

$2(-3x+3)^2 - 84x - 4(-3x+3) + 138 = 0$
 $2(9x^2 - 18x + 9) - 84x + 12x - 12 + 138 = 0$
 $18x^2 - 36x + 18 - 84x + 12x - 12 + 138 = 0$
 $18x^2 - 108x + 144 = 0$
 $18(x^2 - 6x + 8) = 0$
 $18(x-4)(x-2) = 0$
 $x = 4, 2$

$y = -3(4) + 3 = -9$
 $y = -3(2) + 3 = -3$

$(4, -9), (2, -3)$

13) $3x^2 + 4y^2 + 123x - 2y = 0$
 $-3x + y = 0 \quad y = 3x$

$3x^2 + 4(3x)^2 + 123x - 2(3x) = 0$
 $3x^2 + 4(9x^2) + 123x - 6x = 0$
 $3x^2 + 36x^2 + 123x - 6x = 0$
 $39x^2 + 117x = 0$
 $39x(x+3) = 0$
 $x = 0, -3$

$(0, 0), (-3, -9)$

10) $6x^2 - 5y^2 - 102x + y - 122 = 0$
 $2x + y = 1 \quad y = -2x + 1$

$6x^2 - 5(-2x+1)^2 - 102x + (-2x+1) - 122 = 0$
 $6x^2 - 5(4x^2 - 4x + 1) - 102x - 2x + 1 - 122 = 0$
 $6x^2 - 20x^2 + 20x - 5 - 102x - 2x - 121 = 0$
 $-14x^2 - 84x - 126 = 0$
 $-14(x^2 + 6x + 9) = 0$
 $-14(x+3)(x+3) = 0$
 $x = -3$

$y = -2(-3) + 1 = 6 + 1 = 7$

$(-3, 7)$

12) $x^2 + y^2 + 30x - y + 14 = 0$
 $2x + y - 3 = 0 \quad y = -2x + 3$

$x^2 + (-2x+3)^2 + 30x - (-2x+3) + 14 = 0$
 $x^2 + 4x^2 - 12x + 9 + 30x + 2x - 3 + 14 = 0$
 $5x^2 + 20x + 20 = 0$
 $5(x^2 + 4x + 4) = 0$
 $5(x+2)(x+2) = 0$
 $x = -2$

$y = -2(-2) + 3 = 7$

$(-2, 7)$

14) $x^2 + y^2 + 12x + 2y - 3 = 0$
 $3x - y = 3 \quad y = 3x - 3$

$x^2 + (3x-3)^2 + 12x + 2(3x-3) - 3 = 0$
 $x^2 + 9x^2 - 18x + 9 + 12x + 6x - 6 - 3 = 0$
 $10x^2 = 0$
 $x^2 = 0$
 $x = 0$

$y = 3(0) - 3 = -3$

$(0, -3)$